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Introduction

Performance Analysis

Performance Optimization

Summary

- Parallel programming is used to increase application performance
 - Parallel applications use multiple cores or even machines
 - Using more resources also increases runtime costs
 - Make sure that resources are used as efficiently as possible
- Parallel computers are complex
 - · Measuring performance is not always straightforward
 - Estimating potential performance is even harder

Motivation...

- There are several goals for performance optimization
 - 1. Minimizing runtime
 - · Allows getting the results as fast as possible
 - Typically the most important factor for users
 - 2. Maximizing throughput
 - Executes as many jobs as possible within a given time
 - Does not necessarily say anything about performance
 - 3. Maximizing utilization
 - Makes the best use of investment for resources
 - Does not necessarily match the above goals
- · Performance measurements are necessary to check goals
 - Measure, assess and optimize

Approaches

Performance Analysis and Optimization

• When doing performance optimization, there is a loop:

- 1. Conduct performance measurements
 - Running the application, measuring time etc.
- 2. Check if performance is satisfactory
 - · Might not have anything to do with actual utilization
 - · Should also check whether performance is already optimal
- 3. Speculate about the reason for the performance problems
 - · Measurements can point you in the right direction
- 4. Fix performance problems
 - You might actually fix something else (or nothing at all)
- This is more or less "debugging for performance"

- There are two major approaches for performance measurements
 - 1. Offline approaches
 - · Record metrics at runtime, write them to storage
 - Analyze performance afterwards
 - 2. Online approaches
 - · Record metrics at runtime, forward them to a tool
 - Analyze performance at runtime
- In practice, the approaches we use are a mix of both

• Benefits

- · Metrics are available for multiple analyses
 - You might want to look at different metrics etc.
- Allows easily comparing multiple runs
- Drawbacks
 - Typically constant overhead for collecting metrics
 - There is often not an easy way to refine collection
 - · If you notice a performance hotspot, you have to rerun the application
 - Metrics can get quite large
 - Up to gigabytes or even terabytes for large applications

• Benefits

- · Allows adapting collected metrics and thus overhead
- · Easy to switch collection on and off
 - Possible to collect performance metrics in production runs
- Drawbacks
 - Typically not possible to analyze performance afterwards
 - · Collected metrics are transient and lost after the application finishes
 - Requires a separate tool that can process online metrics
 - This also makes the whole approach more complex

Introduction

Performance Analysis

Performance Optimization

Summary

- It is difficult to measure performance correctly
 - There are many factors and components to consider
 - Random errors can influence results significantly
 - · Systematic errors can invalidate all results
- Measuring performance is a complex process
 - Performance is influenced by caching, network, I/O etc.
 - Which components are involved and have to be measured?
 - Which performance can we expect on a given system?

- Optimization requires deep knowledge of the hardware
 - How do the different levels of caches interact?
 - Can we reach the main memory from all cores with the same speed?
 - · How does our application behave with more cores?
- · There are also technical issues to take into account
 - · HPC applications are typically run via a batch scheduler
 - Operating system services can influence performance

- · Our goal is to collect metrics quantitatively
 - · Metrics include runtime, throughput, latency and more
 - The metrics to collect depend on the software and hardware
- · Published measurements should be scientifically sound
 - · Other scientists should be able to reproduce your findings
 - · Measurements of metrics have errors that have to be accounted for
- Results always vary slightly even for the same configuration

- Application A runs for 4.274 s, application B for 4.176 s. Which one is faster?
 - 1. Application A
 - 2. Application B
 - 3. Difference is negligible, performance is the same
 - 4. Not enough information

- Single measurements are more or less random
 - Processor might be busy with something else
 - Some other application is currently occupying the network
 - There is a certain variability for each component
- · It is never enough to do a single measurement
 - Always repeat measurements at least three times
 - If you talk to physicists, they will probably say 30 times
- · Averaging the metrics is also not enough
 - There are important derived metrics, such as standard deviation etc.

Measurements...

```
Benchmark #1: ./sincos-02
   Time (mean +- sig): 4.192 s +- 0.033 s [User: 4.181 s, System: 0.001 s]
2
3
   Range (min .. max): 4.160 s .. 4.274 s 10 runs
4
5
   Benchmark #2: ./sincos-03
   Time (mean +- sig): 4.191 s +- 0.016 s [User: 4.179 s, System: 0.001 s]
6
7
   Range (min .. max): 4.176 s .. 4.221 s 10 runs
8
9
   Summarv
10
   './sincos-03' ran
11
       1.00 + - 0.01 times faster than './sincos-02'
```

- Application A and B have the same performance
 - Both previous results were extreme values (minimum and maximum)

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Performance Analysis and Optimization

- There are two kinds of errors
 - 1. Random errors
 - Cancel out after infinite measurements
 - · Might be caused by operating system activity in the background
 - · Performance of most hardware varies a bit
 - Larger variations are also possible due to hardware defects, load balancing etc.
 - 2. Systematic errors
 - · These errors do not cancel out with more measurements
 - They are caused by wrong methodology/implementation
 - For instance, you want to measure disk speed but measure the cache

- · Always use a well-defined hardware/software environment
 - Document the setup, including version numbers etc.
- · Minimize external influence to keep random errors low
 - Use resources exclusively if possible
 - · For example, do not run anything in the background
- · Increase measurement time and repeat measurements
 - This helps canceling out random errors
- Compare results with expected performance
 - "My application finishes in two hours. Could it finish in one?"
 - This typically involves some kind of performance modeling

• Twelve Ways to Fool the Masses When Giving Performance Results on Parallel Computers by David Bailey [Bailey, 1991]

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- 11. "Measure parallel run times on a dedicated system, but measure conventional run times in a busy environment."

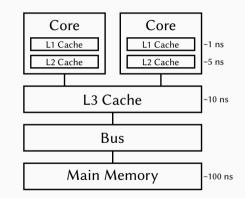
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- 9. "Quote performance in terms of processor utilization, parallel speedups or MFLOPS per dollar."
- 11. "Measure parallel run times on a dedicated system, but measure conventional run times in a busy environment."
- 12. "If all else fails, show pretty pictures and animated videos, and don't talk about performance."

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Performance Analysis and Optimization

- The simplest performance metric: Wall-clock time (or real time)
 - Measure how long the application runs
- There are different kinds of times
 - CPU time denotes the time the processor spent running the application
 - Can be lower or higher than wall-clock time
 - Lower: Two applications share a core, that is, each gets 50 % of CPU time
 - Higher: An application runs on ten cores for one hour, that is, for ten CPU hours
 - User time denotes the time spent in user mode
 - This counts normal calculations etc.
 - System time denotes the time spent in kernel mode
 - This counts system calls, such as I/O

- · Numerous reasons for performance problems
- Inefficient access to resources
 - These are often caused by latencies
 - Data not available in fastest cache
 - Main memory is relatively slow
 - Indirect memory access
- Access conflicts on shared resources
 - Multiple applications want to access the bus
 - · File systems are typically shared



- · Processor utilization is often not optimal
 - Sometimes only 1–10 % are used, especially for parallel applications
 - · Parallel applications have communication and synchronization overhead
- Scientific software is often not well-optimized
 - Domain scientists are interested in scientific results, not optimizing software
 - · Domain scientists often do not have a computer science background
 - Best case: Domain scientist + mathematician/physicist + computer scientist

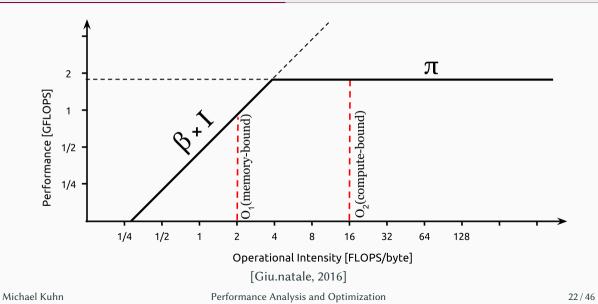
- Application-specific limitations
 - CPU-bound: Limited by processor
 - · For instance, processor cannot do more floating point operations
 - · Could be solved by increasing the clock rate or adding more floating point units
 - Memory-bound: Limited by memory
 - Data cannot be transferred from the main memory to the processor fast enough
 - Typically caused by not doing enough operations per transferred byte
 - I/O-bound: Limited by storage and/or network
 - Data cannot be transferred to/from storage fast enough
- Unrealistic performance gains, such as superlinear speedup
 - For instance, making the problem smaller allows it to fit into the cache

Theoretical

- Determine time and memory complexity
- Can be impractical for general applications
- · Helps to have at least a rough understanding of complexity
 - Get a feeling for potential runtime/memory consumption
- Practical
 - · Measure time and memory consumption
 - Relatively easy to do with the right tools
- A combination of both approaches makes most sense

- One way to assess performance is the so-called roofline model
 - Visual representation of performance limits in current architectures
 - Requires finding out peak memory throughput and computational performance
 - · Application's operational intensity has to be determined
 - Can be extended using other factors important for performance
- The performance metric given most attention in HPC is FLOPS
 - FLOPS = Floating point operations per second
 - Different metrics are discussed since FLOPS are only one aspect

Roofline Model...



Introduction

Performance Analysis

Performance Optimization

Summary

- The overall goal is to optimize resource usage
 - · This applies to all involved components
 - · Processor, storage, network etc. require different approaches
- · Resources are typically used exclusively in HPC
 - There are exceptions; for example, the file system is shared
 - Problems cannot be compensated by running additional applications
 - · Users should make sure that they do not underutilize resources
- · Also important for shared resources
 - Worst case: A single application can bring down performance for everyone
 - Applications should not overload the file system

- We will focus on the computational performance for now
 - · Moreover, we will mainly look at numerical applications
- 1. Optimize the mathematics and algorithms
 - · Requires the most knowledge about the problem
 - Should rather be done by a domain scientist and/or mathematician
- 2. Optimize the code manually
 - Determine which data structures and algorithms are best suited
 - Vectorization can be a huge performance benefit
 - Take software and hardware characteristics into account
 - How much main memory is available? How does the compiler align/order data?
- 3. Optimize the code automatically
 - The compiler can take care of a lot of optimizations for us

- The programming language can also have a huge influence on performance
 - In the end, use the language you are most comfortable with
 - Using a new language will not automatically make your application faster
- There is a wide range of programming languages to choose from
 - C, C++, Fortran, Python, Java, MATLAB etc.
- · Some languages are better suited for specific problems
 - For example, good data science and machine learning support for Python

- C (which we will use in the lecture and exercises)
 - Allows low-level programming and direct access to the hardware
 - · Requires you to take care of memory management yourself
 - Compilers are mature and produce efficient code
 - · Most functionality like threading is supported
 - · A lot of performance-critical libraries and framework are written in C
- C++
 - More or less the same benefits and drawbacks as C with a nicer syntax
 - More convenient memory management than C
- Fortran (from Formula Translation)
 - Easier to handle for non-computer scientists
 - Has a long history and is still updated frequently

• Python

- · Very popular right now and has a huge community
- · Many modules are available, providing a lot of features
- · Standard version is interpreted and thus slow
 - There are a number of modules written in C for high performance
- There is no easily usable threading support
- Java
 - · Popular in industry, large community and many features
 - Byte code can be optimized at runtime

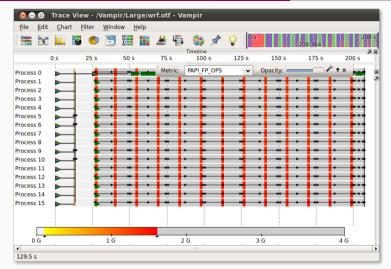
- Time measurement
 - time and /usr/bin/time are available everywhere
 - Can also be done manually using, for example, clock_gettime
- Profiling
 - gprof can be used to display application profiles
- Dedicated performance analysis
 - · perf is part of the Linux kernel and features many dedicated metrics
- Graphical applications
 - Vampir is a commercial tool to display traces and profiles

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Process 15				-				•	*		•		

[GWT-TUD GmbH, 2020]

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Tools...



[GWT-TUD GmbH, 2020]

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- Simple numerical application
 - Nested loop with calculations
- Two complex operations
 - Plus two simple operations
- Performance expectations
 - sin and cos are expensive
 - Maximum is hard to judge

```
int main (void) {
    double result = 0.0;
    for (int i = 0; i < 20000; i++) {
        for (int j = 0; j < 20000; j++) {
            result += sin(i) + cos(j);
        }
    }
    printf("result=%f\n", result);
    return 0;
}</pre>
```

Performance Analysis and Optimization

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```
1 $ time ./sincos
2 result=10120.671812
3 ./sincos 8.88s user 0.00s system 99% cpu 8.896 total
4 
5 $ /usr/bin/time ./sincos
6 result=10120.671812
7 8.88user 0.00system 0:08.89elapsed 99%CPU (... 2132maxresident)k
8 0inputs+0outputs (0major+78minor)pagefaults 0swaps
```

- time is a shell built-in
 - /usr/bin/time is a regular system tool
- · Both show user, system and total time as well as processor utilization
 - /usr/bin/time also provides memory consumption etc.

- Profiling using gprof does not help in this case
 - Everything is contained in the main function
- Compile the application with the -pg flag
 - Running it will automatically produce a profile called gmon.out
- Most of the time is probably spent in sin and cos

```
$ gprof ./sincos
2
  Flat profile:
3
4
  Each sample counts as 0.01 seconds.
5
    %
        cumulative self
                                      self
                                          total
          seconds seconds calls Ts/call Ts/call
6
   time
                                                      name
7
  101.86
         0.81
                      0.81
                                                      main
```

Tools...

1	<pre>\$ perf stat ./sinco</pre>	0S			
2	result=10120.671812	2			
3	Performance counte	er stats for './sincos':			
4	9,016.15	<pre>msec task-clock:u</pre>	#	0.998	CPUs utilized
5	0	context-switches:u	#	0.000	K/sec
6	0	cpu-migrations:u	#	0.000	K/sec
7	68	page-faults:u	#	0.008	K/sec
8	37,667,245,120	cycles:u	#	4.178	GHz
9	46,473,927	stalled-cycles-frontend:u	#	0.12%	frontend cycles idle
10	23,374,754,930	stalled-cycles-backend:u	#	62.06%	backend cycles idle
11	89,573,942,974	instructions:u	#	2.38	insn per cycle
12			#	0.26	stalled cycles per insn
13	11,597,942,217	branches:u	#	1286.352	M/sec
14	45,071,449	branch-misses:u	#	0.39%	of all branches
15	9.035267264	seconds time elapsed			
16	9.013823000	seconds user			
17	0.00000000	seconds sys			

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- · perf shows a number of different performance metrics
 - Runtime is just one of them
- · Context switches occur when talking to the kernel
 - · They are relatively fast but should be taken into account
- · CPU migrations can have negative influence on caching
 - Moving the application to another core or processor will invalidate caches
- Cycles and instructions show how much the processor had to do
 - · Modern processors can do multiple instructions per cycle
- Branches can be bad for performance if there are many misses

- · Compilers can do a lot of optimizations for us
 - Can also be tuned for specific architectures
 - · Takes instruction sets, number of registers etc. into account
- -00
 - · Default, no optimizations are performed
- -01
 - · Basic optimizations, compilation requires more time and memory
- -02
 - · More optimizations, often used as the "default" optimization
- -03
 - Even more optimizations, including vectorization

- -0g
 - Optimize for debugging, some important passes are disabled at -00
- -0s
 - Optimize for size, good for embedded systems with little storage
- -Ofast
 - · Optimize by disregarding standards compliance, might influence results

- Inlining allows avoiding function calls (starting from -01)
 - Function calls require putting arguments onto the stack
 - · Afterwards, there are jumps into the function and back to the original location
- Loop unrolling (-03)
 - · Loops also require jumps, which can be negative for performance

```
for (int i = 0; i < 3; i++) {

a[i] += b[i];

}

1 a[0] += b[0];

\rightarrow 2 a[1] += b[1];

3 a[2] += b[2];
```

- Vectorization can perform multiple operations at once (-03)
 - · Especially useful in combination with loop unrolling

- Which speedup can we get for our application with compiler optimizations alone?
 - 1. None
 - 2. Factor 10
 - 3. Factor 100
 - 4. Factor 1,000

Compilers...

<pre>\$ perf stat ./sinco result=10120.671812</pre>		
Performance counte	r stats	for './sincos':
9,016.15	msec tas	sk-clock:u
0	COI	ntext-switches:u
0	сри	u-migrations:u
68	pa	ge-faults:u
37,667,245,120	су	cles:u
46,473,927	sta	alled-frontend:u
23,374,754,930	sta	alled-backend:u
89,573,942,974	in	structions:u
11,597,942,217	bra	anches:u
45,071,449	bra	anch-misses:u
9.035267264	seconds	time elapsed
9.013823000	seconds	user
0.00000000	seconds	sys

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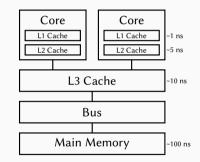
Compilers...

<pre>\$ perf stat ./sincos</pre>	s – 03	<pre>\$ perf stat ./sinco</pre>	DS			
result=10120.671812		result=10120.671812				
Performance counte	r stats for './sincos':	Performance counte	er stats for './sincos':			
4,278.80	msec task-clock:u	9,016.15	msec task-clock:u			
0	context-switches:u	0	context-switches:u			
0	cpu-migrations:u	0	cpu-migrations:u			
67	page-faults:u	68	page-faults:u			
17,886,687,516	cycles:u	37,667,245,120	cycles:u			
19,370,964	stalled-frontend:u	46,473,927	stalled-frontend:u			
11,376,027,366	stalled-backend:u	23,374,754,930	stalled-backend:u			
45,200,173,879	instructions:u	89,573,942,974	instructions:u			
6,000,368,555	branches:u	11,597,942,217	branches:u			
19,211,736	branch-misses:u	45,071,449	branch-misses:u			
4.288728446	seconds time elapsed	9.035267264	seconds time elapsed			
4.278149000	seconds user	9.013823000	seconds user			
0.00000000	seconds sys	0.00000000	seconds sys			
	result = 10120.671812 Performance counte 4,278.80 0 0 67 17,886,687,516 19,370,964 11,376,027,366 45,200,173,879 6,000,368,555 19,211,736 4.288728446 4.278149000	result=10120.671812 Performance counter stats for './sincos': 4,278.80 msec task-clock:u 0 context-switches:u 0 cpu-migrations:u 67 page-faults:u 17,886,687,516 cycles:u 19,370,964 stalled-frontend:u 11,376,027,366 stalled-backend:u 45,200,173,879 instructions:u 6,000,368,555 branches:u	result=10120.671812 Performance counter stats for './sincos': 4,278.80 msec task-clock:u 0 context-switches:u 0 cpu-migrations:u 67 page-faults:u 17,886,687,516 cycles:u 19,370,964 stalled-frontend:u 11,376,027,366 stalled-backend:u 45,200,173,879 instructions:u 6,000,368,555 branches:u 11,597,942,217 19,211,736 branch-misses:u 4.288728446 seconds time elapsed 4.278149000 seconds user result=10120.671812 Performance counter 9,016.15 Performance counter 9,016.15 0 20,016,15 0 21,507 11,507,942,217 11,597,942,217 45,071,449 9,035267264 9,013823000			

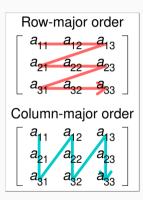
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- This time, sincos was compiled with -03
 - Runtime was more than halved from 9 s to 4.3 s
 - · Cycles, instructions and branches were roughly halved
 - Instructions per cycle went up slightly
- Teaser: -Ofast achieves a runtime of only 1.5 s
 - -Ofast also requires linking with libmvec, that is, uses vectorization
 - Optimizing for the architecture with -march=native gets it down to 0.5 s

- Memory access and caches important for performance
 - · Access to main memory takes approximately 100 ns
 - At 3 GHz (at least) 300 instructions in 100 ns
- · Caches can help get data to the processor fast enough
 - Processors will speculatively load data into the cache
 - Typically assume spatial locality, that is, nearby memory will be accessed in the future
- · Caches work well if you access data the right way
 - Jumping around randomly will destroy locality



- Memory access depends on the programming language
 - C stores memory in row-major order
 - · Fortran stores memory in column-major order
- · Access in the wrong order will reduce performance
 - · Has to be considered when porting code
- Combining programming languages can be problematic
 - For instance, using a C library from Fortran



[Cmglee, 2017]

• C application with row-major matrix

Memory Access...

- Still potential performance problems
- Gray cells contain calculation values
 - · Blue cells are loaded into cache
 - CPU-bound given enough math

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

- C application with row-major matrix
 - Still potential performance problems
- Gray cells contain calculation values
 - · Blue cells are loaded into cache
 - CPU-bound given enough math
- White cells are empty
 - · Values are still loaded into cache
 - · Memory-bound due to unused values
- Special data structures for efficient access to sparse matrices

1	2								
11	12	13							
	22	23	24						
		33	34	35					
			44	45	46				
				55	56	57			
					66	67	68		
						77	78	79	
							88	89	90
								99	100

- Memory interleaving
 - Important for performance
- Array of structures
 - Intuitive representation
 - · Potentially bad cache utilization

```
struct coordinate
2
    {
3
        double x;
        double y;
4
        double z;
5
6
   };
7
   int main (void) {
8
        struct coordinate e[N] = { 0 };
9
        double result = 0.0;
10
        for (int i = 0; i < N; i++)
12
        {
            result += e[i].x * e[i].y;
13
14
        }
15
        return 0;
16
    }
```

- Memory interleaving
 - Important for performance
- Array of structures
 - Intuitive representation
 - Potentially bad cache utilization
- Structure of arrays
 - · Potentially better for vectorization

```
struct coordinates
{
    double x[N];
    double y[N];
    double z[N];
};
int main (void) {
    struct coordinates e = { 0 };
    double result = 0.0;
    for (int i = 0; i < N; i++)
    {
        result += e.x[i] * e.y[i];
    }
    return 0;
```

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Performance Analysis and Optimization

Introduction

Performance Analysis

Performance Optimization

Summary

- There is a range of approaches and tools to find performance problems
 - Parallel computers and applications are complex
- · Performance measurements require a thought-out approach
 - Single measurements can be more or less random
- · Performance optimizations can be done on several levels
 - · Code optimizations can be done manually or automatically
- Compilers often can take care of sophisticated optimizations
 - It is important to understand the compiler's capabilities

References

- [Bailey, 1991] Bailey, D. (1991). Twelve ways to fool the masses when giving performance results on parallel computers. *Supercomputing Review*, pages 54–55.
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Approaches

• O(1)

- Constant runtime/memory consumption
- Example: Array access, hash tables
- O(n)
 - Linear runtime/memory consumption
 - Touch every data point once (or a few times) 4
 - Example: Calculating the sum of a list
- O(n²)
 - Quadratic runtime/memory consumption
 - Example: (Bad) sorting algorithms

for	(int i = 0; i < n; i++) {
	for (int $j = 0; j < n; j++$) {
	result += sin(i) + cos(j)
	}
}	

3